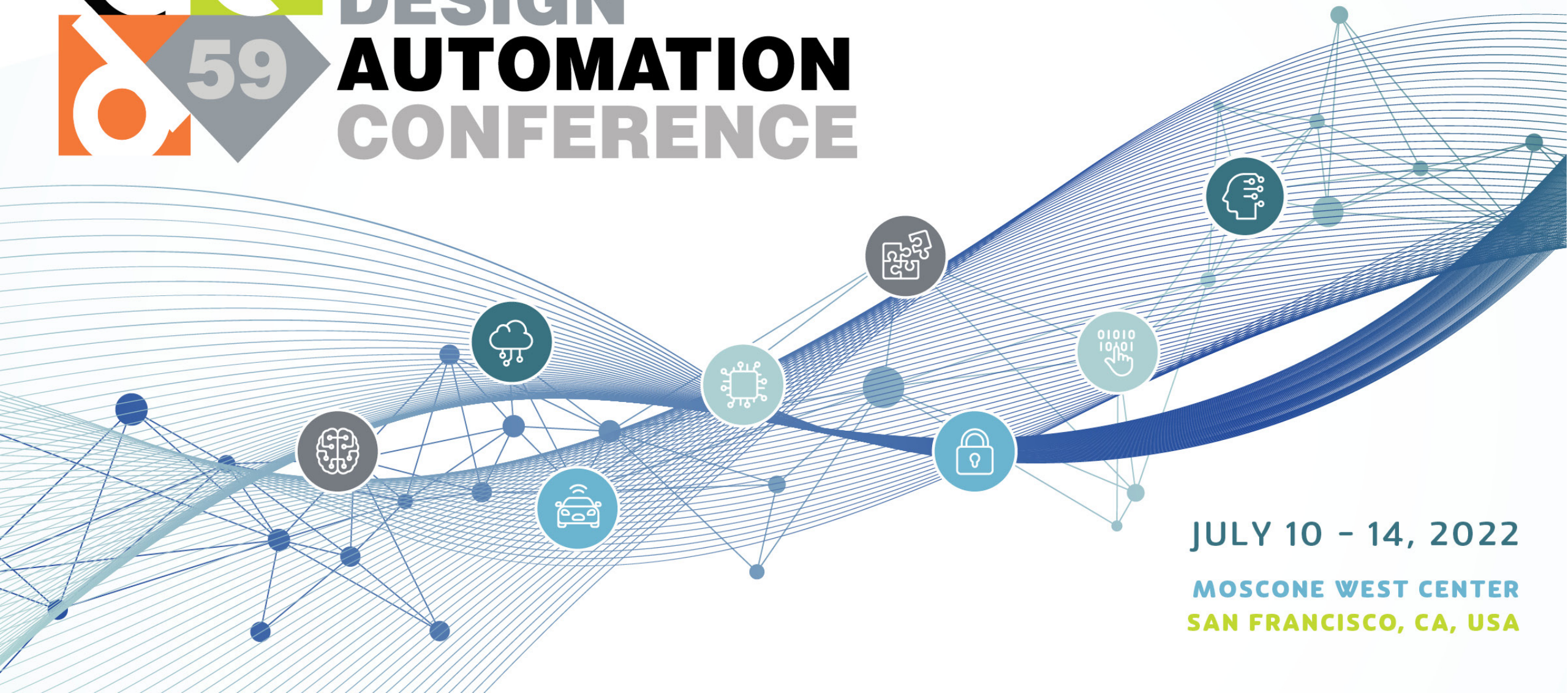




DESIGN **AUTOMATION** CONFERENCE



JULY 10 - 14, 2022

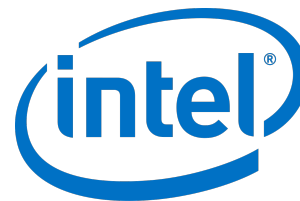
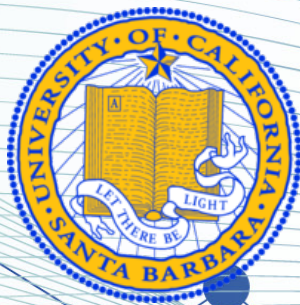
MOSCONE WEST CENTER
SAN FRANCISCO, CA, USA



Enabling Deeper Quantum Compiler Optimization at High Level

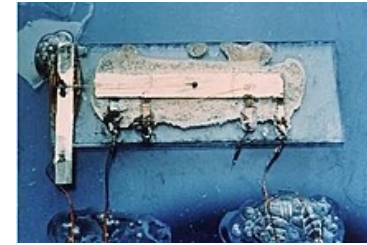
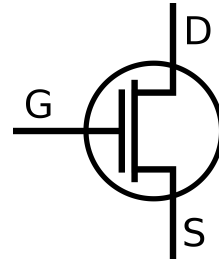
Yufei Ding, Gushu Li, Anbang Wu, Yuan Xie

07/11/2022



The Quantum Revolution

1st Quantum
Revolution



Classical
Computer

1900
Quantum
Mechanics

1947
Transistor

1956
MOSFET

1958
Integrated
Circuit

1980

2nd Quantum Revolution: the power of
quantum is not fully exploited

The Quantum Revolution



2nd Quantum
Revolution

1980
Quantum
Computer

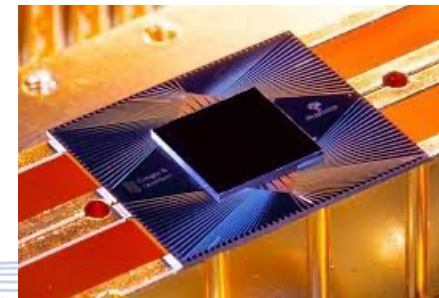
1994
Cryptography

2019
Supremacy

Practical
Quantum
Computing

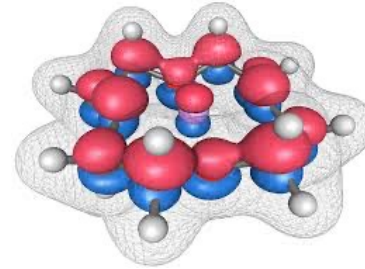


Now

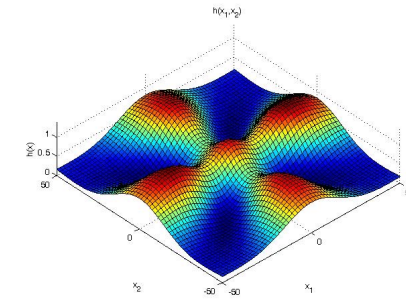


Quantum Computing System Stacks

Application



Simulation



Optimization



Machine Learning



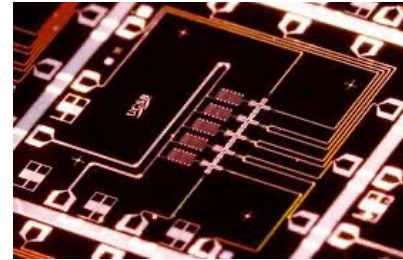
Cryptography

Technology Stacks

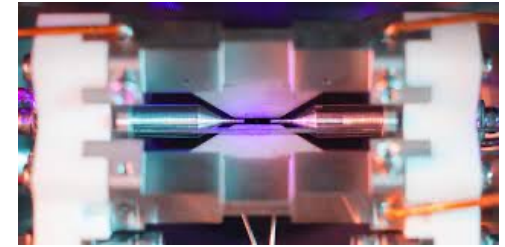
Quantum Computing System Stacks



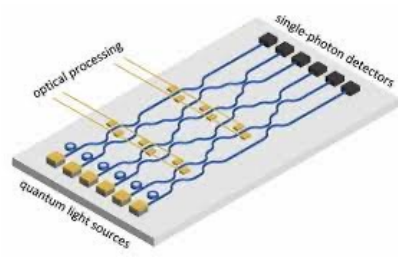
Application



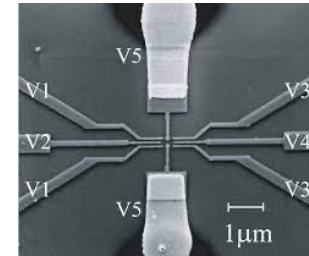
Superconducting



Ion Trap



Photonics



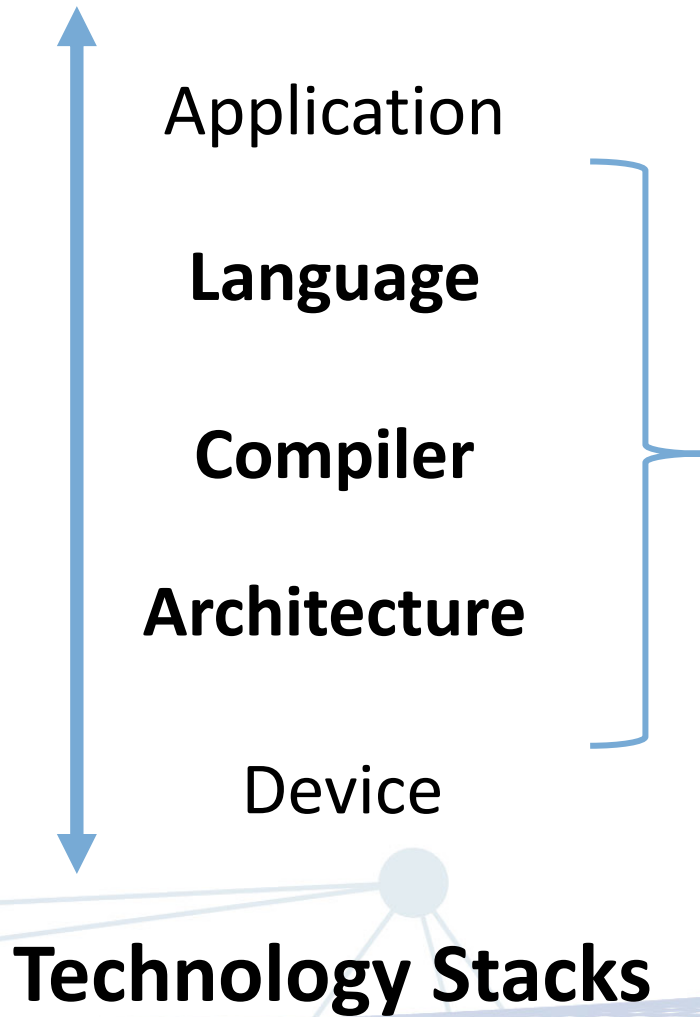
Quantum Dot

Device

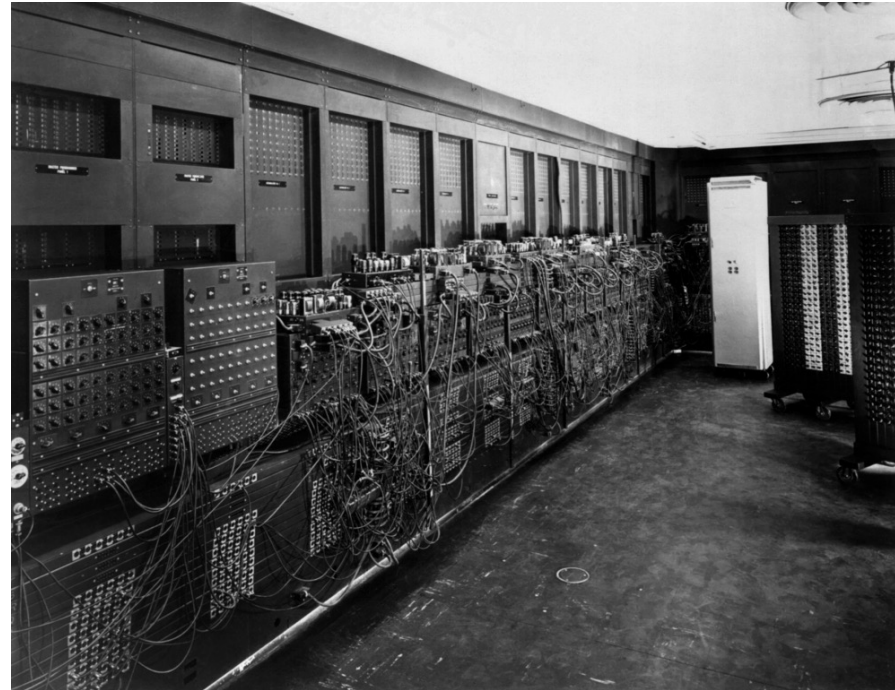


Technology Stacks

Quantum Computing System Stacks

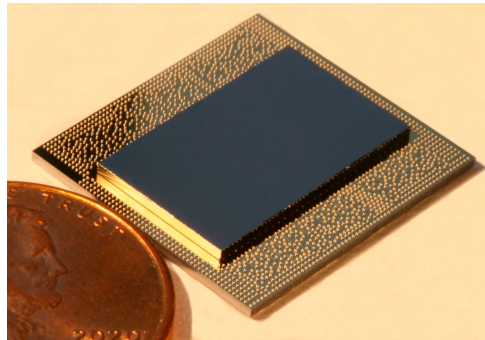


ENIAC, the first electronic general purpose digital computer, 1945

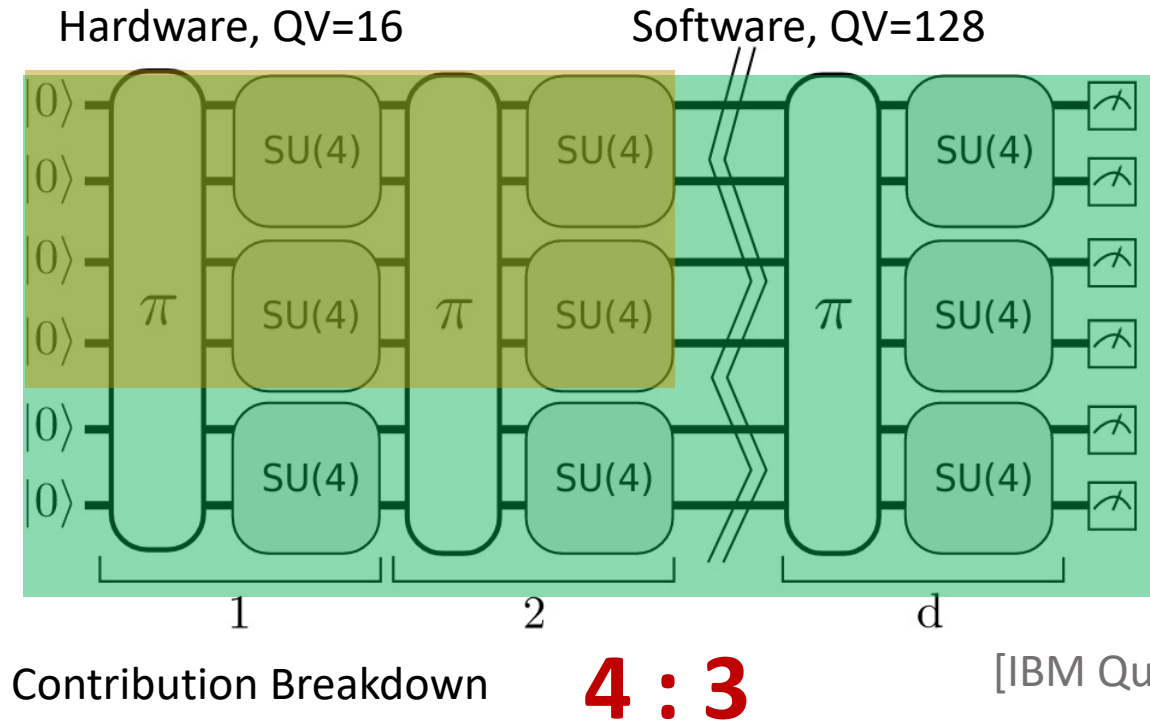


Hardware vs Software

- IBM benchmarking results



IBM Q Montreal



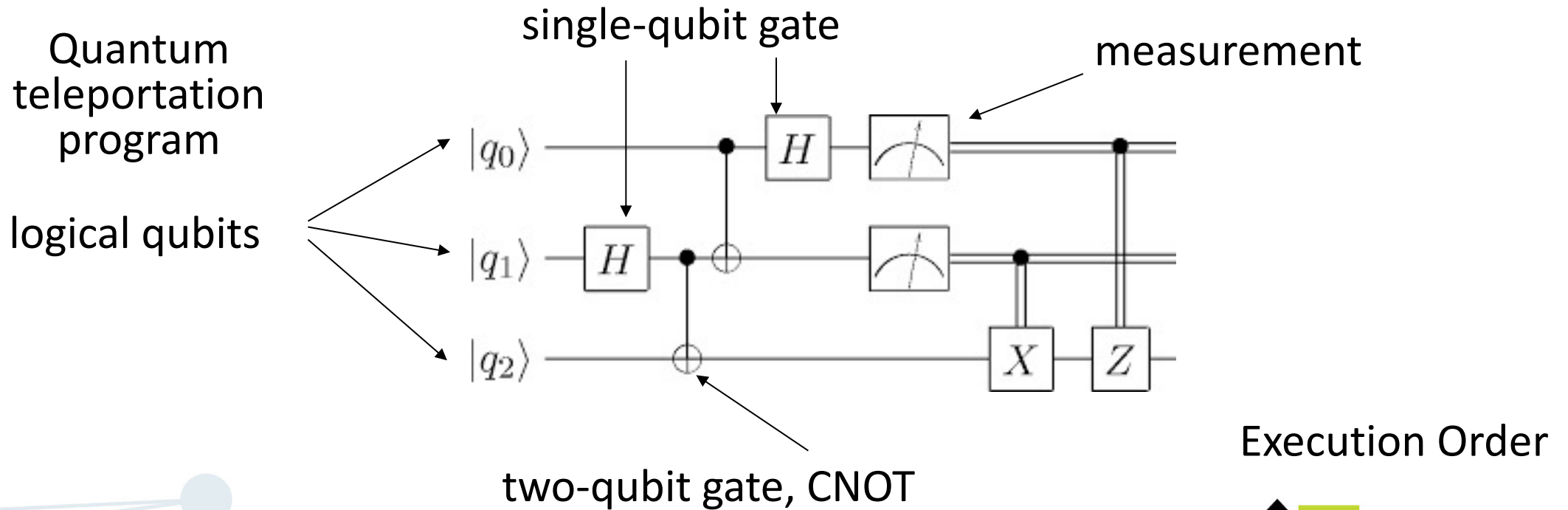
Quantum system research extends the computation capability!

And both software and hardware are important

Quantum Volume (QV): the size of Hilbert space that a quantum processor can explore reliably

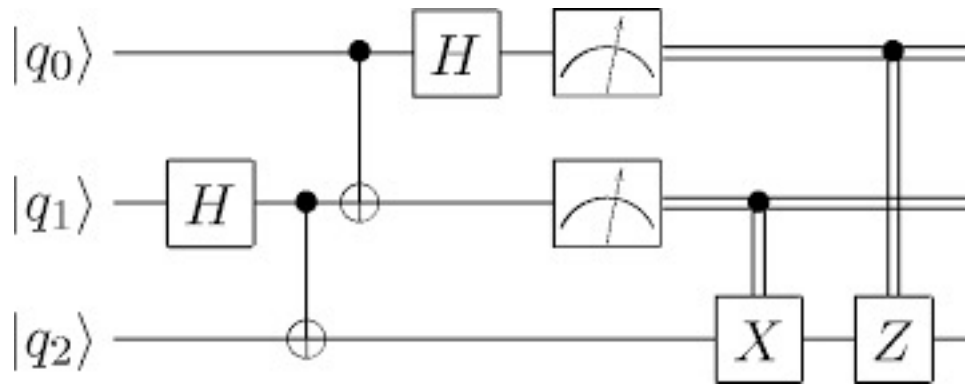
Background

- Quantum software – quantum circuit



Background

- Quantum software – program state



State vector:

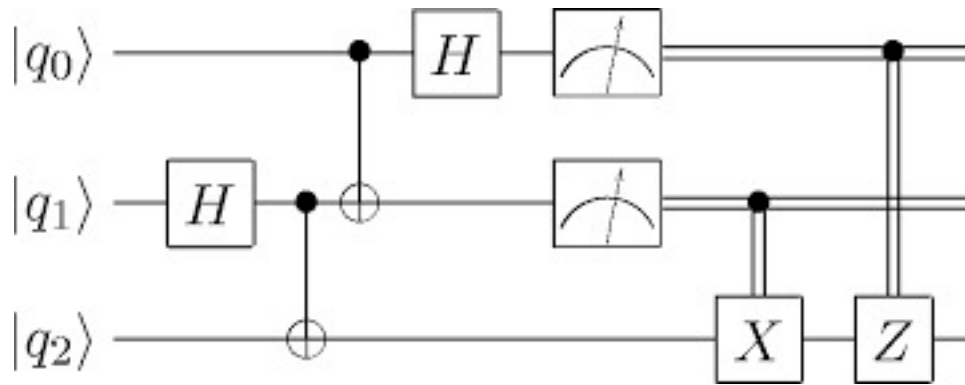
1-qubit, $|\psi\rangle = a_0|0\rangle + a_1|1\rangle$, $[a_0, a_1]$

3-qubit, $|\psi\rangle = a_{000}|000\rangle + a_{001}|001\rangle + \dots + a_{111}|111\rangle$
 $[a_{000}, \dots, a_{111}]$

n-qubit, state vector $[a_0, \dots, a_{2^n-1}]$ of size 2^n

Background

- Quantum software – program semantics



Gate matrices:

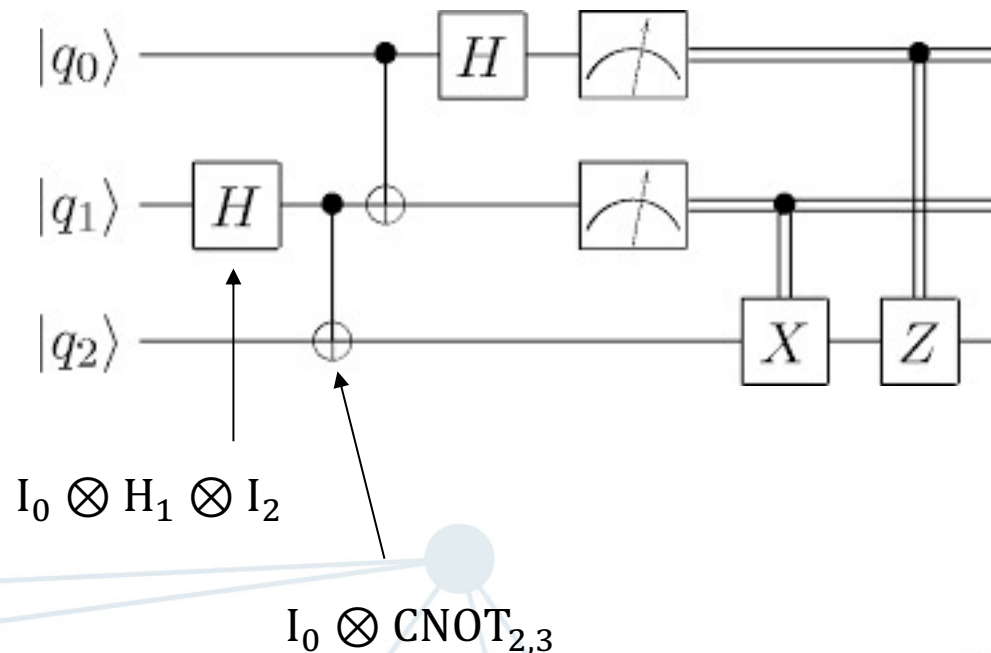
$$\text{1-qubit, } H = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$\text{2-qubit, CNOT} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

n-qubit, matrices of size 2^n by 2^n

Background

- Quantum software – program semantics



Gate matrices:

$$\text{1-qubit, } H = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

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n-qubit, matrices of size 2^n by 2^n

Background

- Quantum hardware – the superconducting architecture

IBM's 5-qubit
superconducting
quantum chip

physical qubits

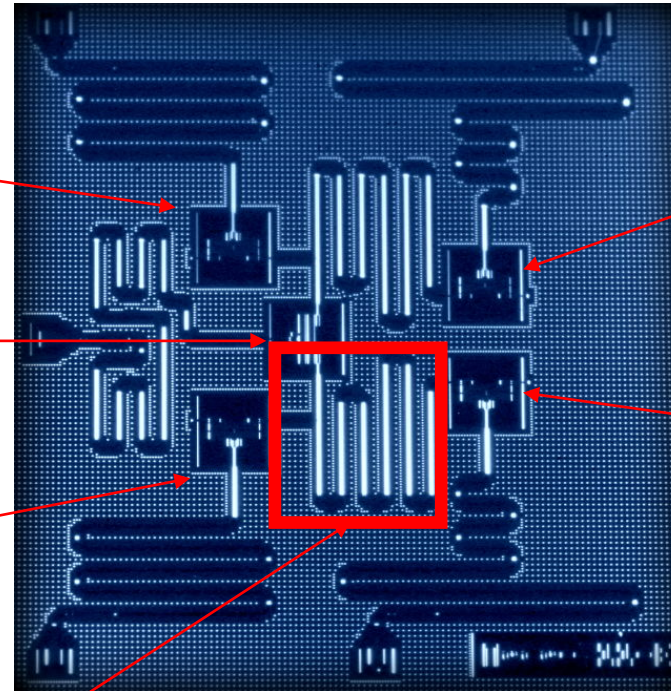
Q3

Q2

Q1

Q4

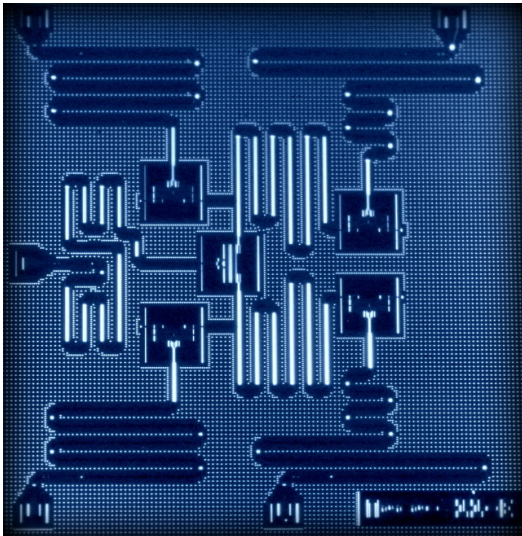
Q0



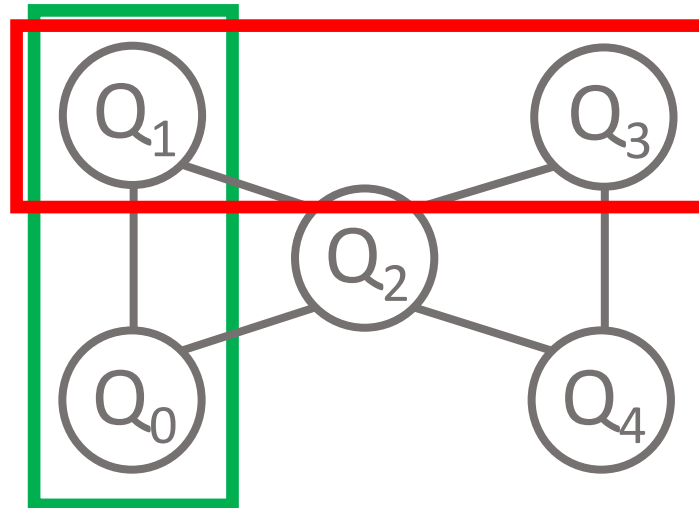
resonator – connect physical qubits

Background

- Quantum hardware – the superconducting architecture



IBM's 5-qubit superconducting quantum chip



Coupling graph – limited qubit connection

CNOT gates only allowed on the connected edges

CNOT Q0, Q1

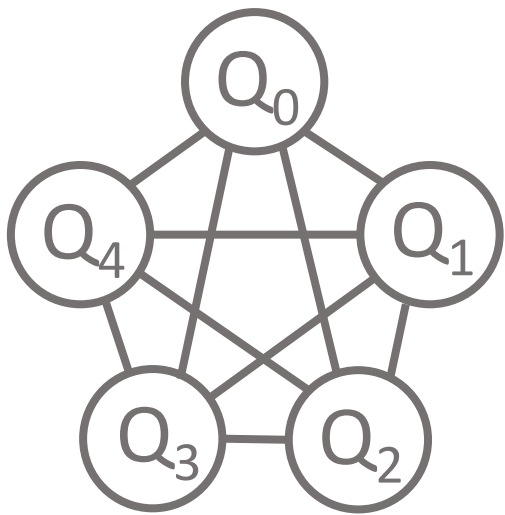


CNOT Q1, Q3

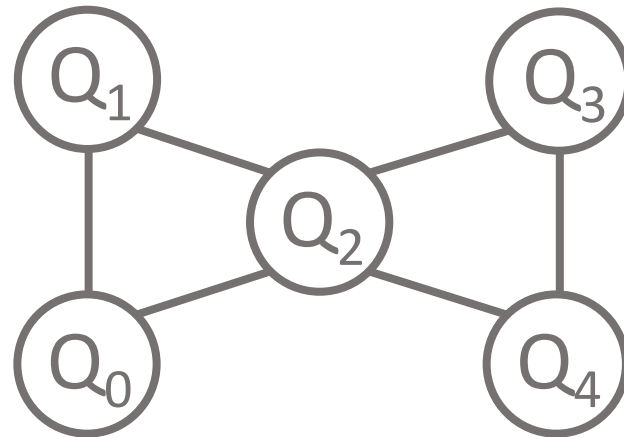
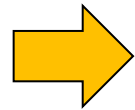


Mismatch

- When we write a quantum program, we may not know the underlying architecture



Ideal device –
complete graph

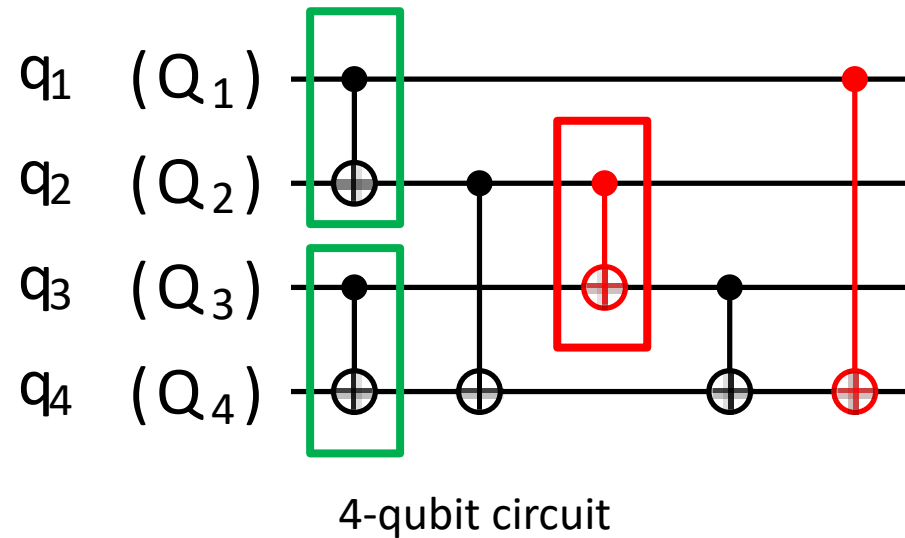
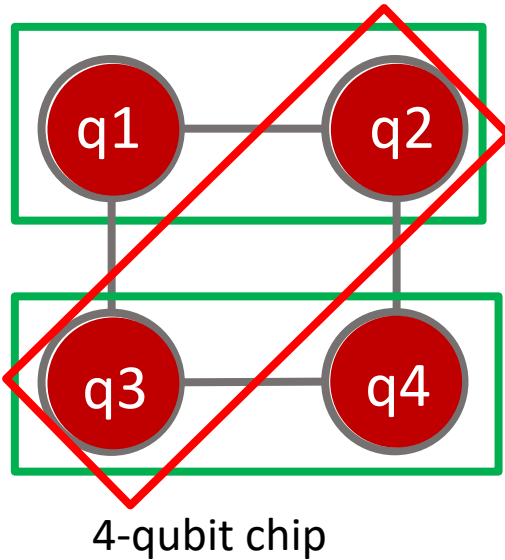


Coupling graph – limited
qubit connection

Some gates may
not be executable

Qubit Mapping

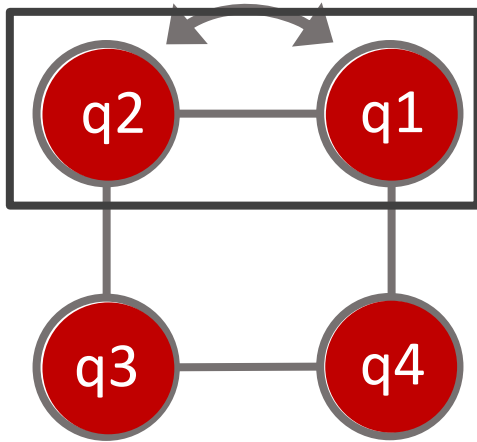
- An Example



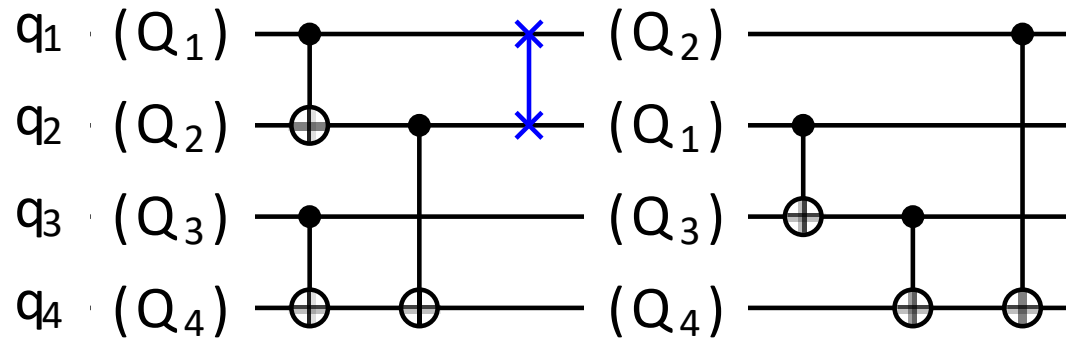
Some CNOTs are executable

Qubit Mapping

- An Example

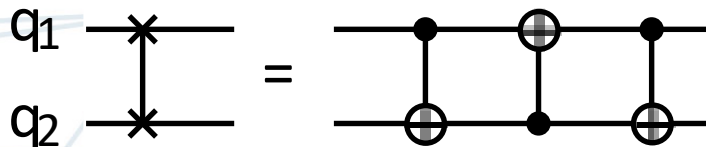


4-qubit chip



Insert additional gate SWAP:
exchange the mapping

4-qubit circuit

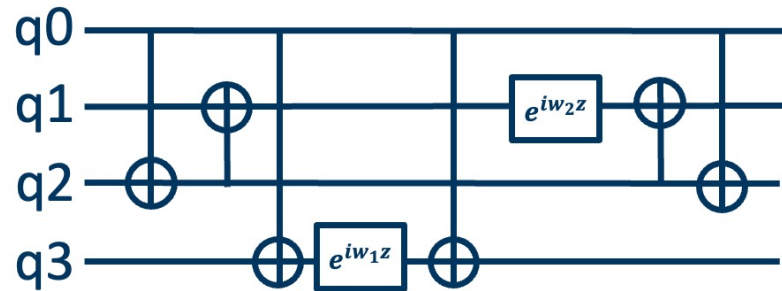


1 SWAP = 3 CNOT

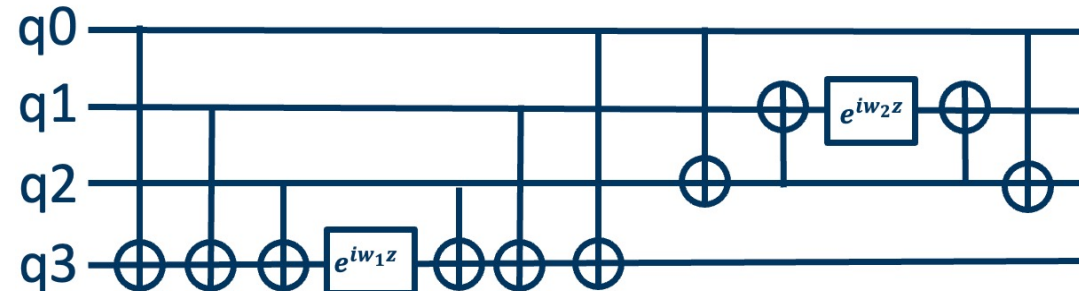
Each additional SWAP leads to more noise

Quantum Compiler Optimization

- Find some circuit identities
- Select the best one according to some metrics (e.g., # gate, # depth) and constraints (e.g., sparse connection on hardware)



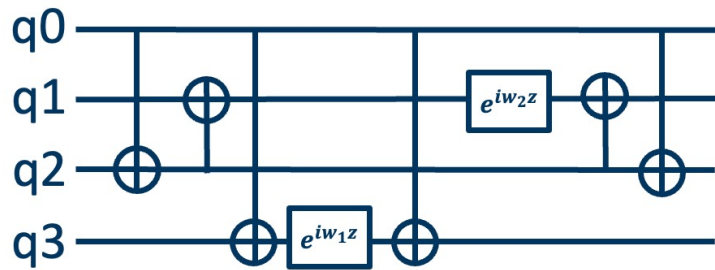
Gate: 6 + 2; Depth: 6



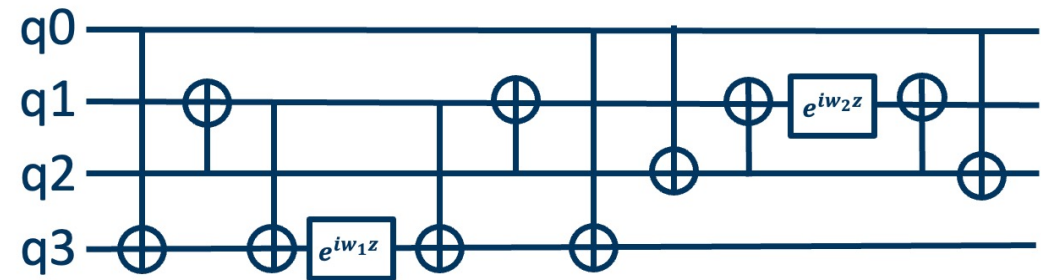
Gate: 10 + 2; Depth: 12

Challenge

- How can we find **large-scale** quantum circuit identities efficiently?



?=



- ❖ Calculate their **matrix representations** and check the **equivalence**?
 - * Scalability issue: Matrix size of $2^n \times 2^n$ and/or huge combinatorial search space.
- ❖ **Limit our compiler optimization scope**: peephole optimization, local swap insertions in qubit mapping, etc.
 - * Missing large-scale optimizations.



Paulihedral: A Generalized Block-Wise Compiler Optimization Framework for Quantum Simulation Kernels

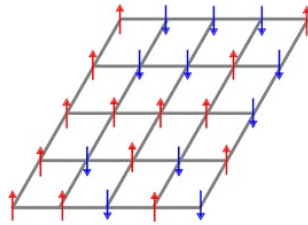
Gushu Li, Anbang Wu, Yunong Shi, Ali Javadi-Abhari, Yufei Ding,
Yuan Xie

ASPLOS 2022

Opportunities at High-Level

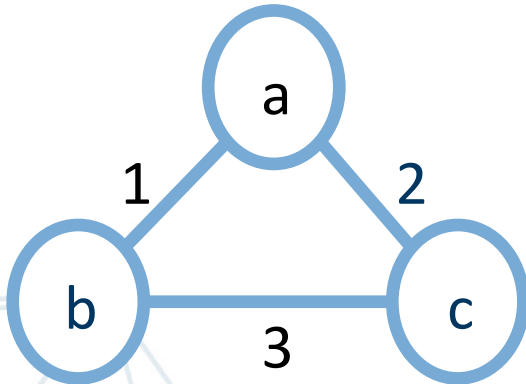
- More **abstract compact** form? Yes
- **Simulation** is widely used in quantum algorithm design

Simulation



$$H = -\sum J_{ij} Z_i Z_j - \mu \sum h_j Z_j$$

Graph Cut



$$H = \frac{1}{2} (Z_a Z_b - I) + \frac{2}{2} (Z_a Z_c - I) + \frac{3}{2} (Z_b Z_c - I)$$

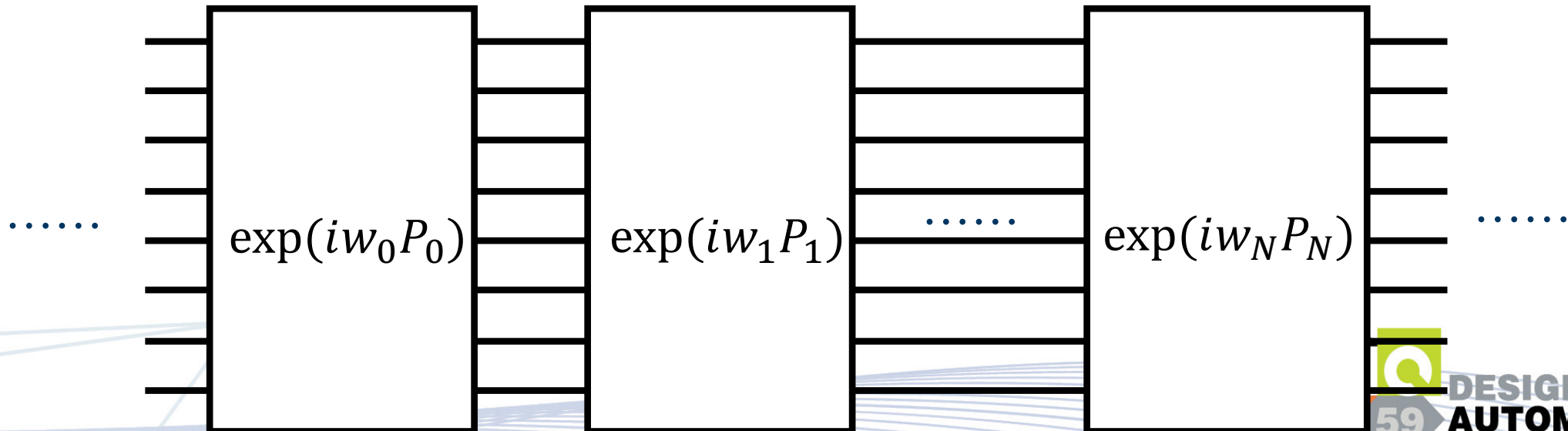
And many more

Quantum Simulation Kernel

- A widely-used subroutine

$$\exp(iHt)$$

$H = \sum_i w_i P_i$, P_i is a Pauli string, $w_i \in \mathbb{R}$ is weight



High-Level IR: Pauli IR

(P, w) Basic unit of our IR: a pair of Pauli string **P** and a real number **w**.

❖ Pauli string **P** is just **Kronecker product** of 1-qubit Pauli matrices (I, X, Y, Z).

$$I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad X = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \quad Y = \begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix} \quad Z = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$

A size-**n** P can concisely express a **2ⁿ x 2ⁿ** matrix

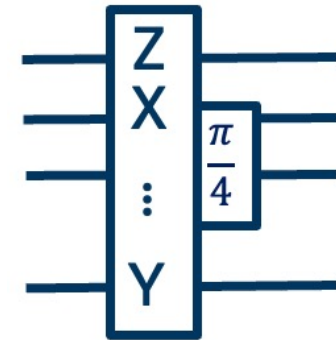
- Examples of 4-qubit Pauli string: $X_3Y_2Z_1I_0$, $Z_3Z_2Z_1Z_0$, $X_3Y_2Y_1X_0$
- **Active qubits** for a Pauli string: qubits with a non-I Pauli matrix.

High-Level IR: Pauli IR

(P, w) denotes a $2^n \times 2^n$ unitary gate $\exp(iwP)$.

Example: $(ZX\dots Y, \frac{\pi}{4}) \longrightarrow \exp(i \frac{\pi}{4} ZX\dots Y)$

Pauli IR (kernel) Exponential form

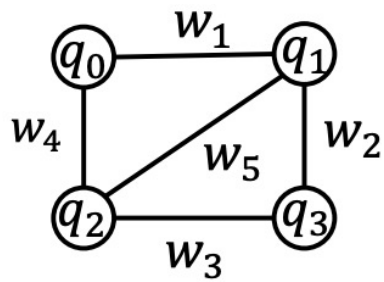


Circuit form

Universal in terms of unitary gates

Compile to Pauli IR

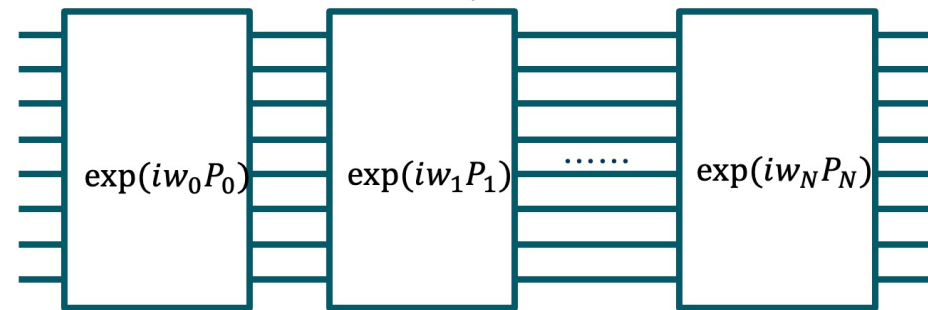
- **Great news:** It is already there, at least for many quantum algorithm design.
- (e.g., QAOA, VQE, and many other quantum simulation algorithms like UCCSD).



$\exp(iw_1 I_3 I_2 Z_1 Z_0 \gamma)$
 $\exp(iw_2 Z_3 I_2 Z_1 I_0 \gamma)$
 $\exp(iw_3 Z_3 Z_2 I_1 I_0 \gamma)$
 $\exp(iw_4 I_3 Z_2 I_1 Z_0 \gamma)$
 $\exp(iw_5 I_3 Z_2 Z_1 I_0 \gamma)$

QAQA Ansatz on graph Max-Cut

$$H = \sum_i w_i P_i$$

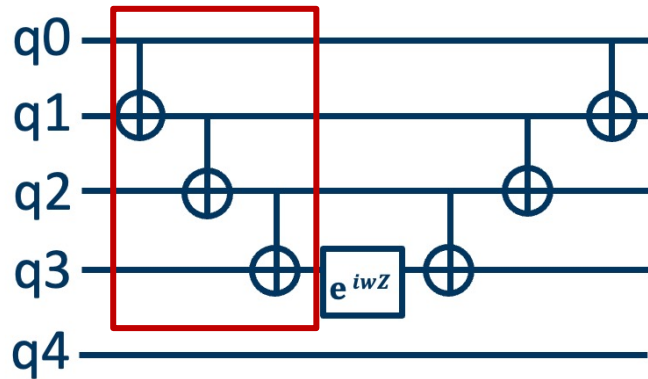


From Pauli IR to Gates

- **Very flexible compilation/synthesis**

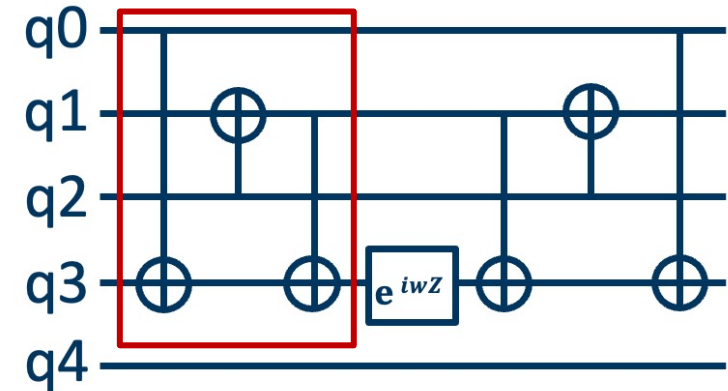
$$\exp(iwI_4Z_3Z_2Z_1Z_0)$$

❖ if **z-basis parity on q3, q2, q1, q0** = 0, apply a global phase $\exp(iw)$; otherwise, apply $\exp(-iw)$.



$q0 \rightarrow q1 \rightarrow q2 \rightarrow q3$

CNOT tree
for parity check



$q0 \rightarrow q3$
 \uparrow
 $q2 \rightarrow q1$

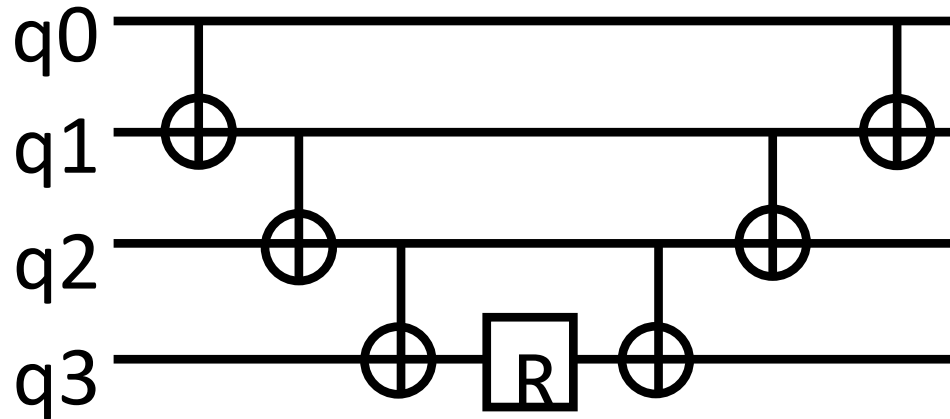
It thus could generate many great **circuit identities** with the same (P, w) .

Example: Qubit Mapping

- How can Paulihedral change the mapping/SWAP insertion?

Conventional Compilation

- Find SWAP in gate sequence



CNOT q0, q1

CNOT q1, q2

CNOT q2, q3



$$\exp(iwZ_3Z_2Z_1Z_0)$$

SWAP q1, ...

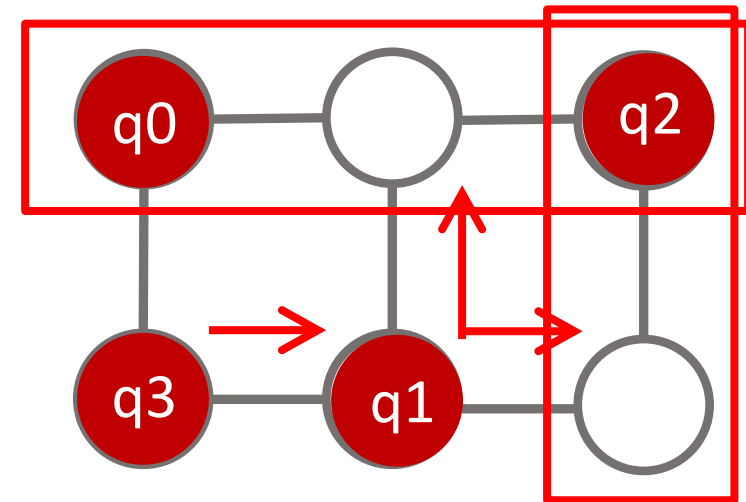
CNOT q0, q1

CNOT q1, q2

SWAP q3, ...

SWAP q3, ...

CNOT q2, q3



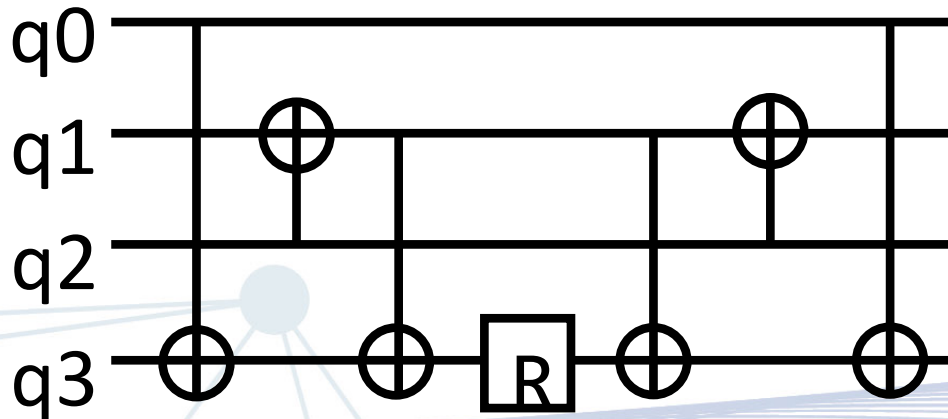
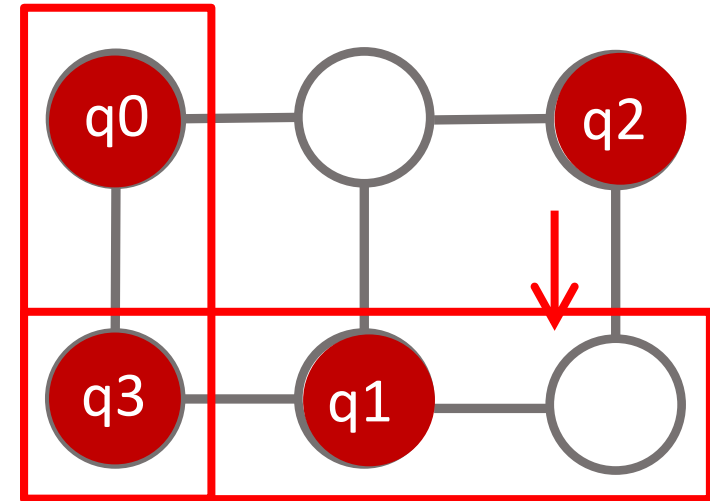
Paulihedral Compilation

- Leverage high-level information

$$\exp(iwZ_3Z_2Z_1Z_0)$$

$$\exp(iwZ_3Z_2Z_1Z_0) \longrightarrow$$

SWAP q2, ...
CNOT q0, q3
CNOT q2, q1
CNOT q1, q3

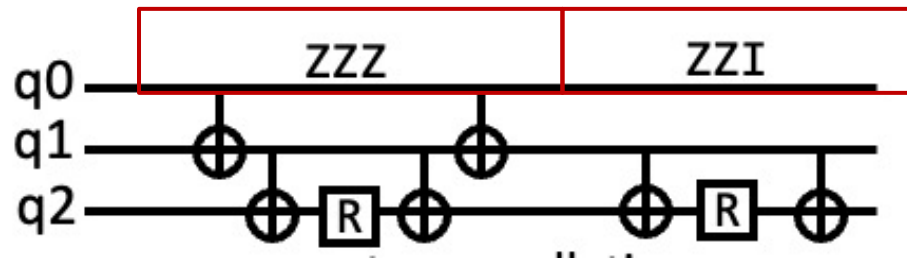


Find a tree embedding, then
generate the CNOT tree

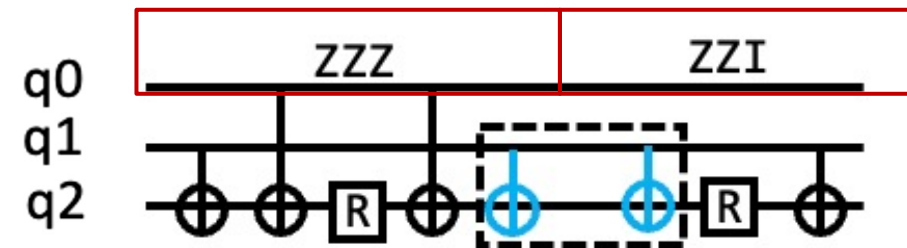
More Gate Cancellation

- Find **global gate cancellation** among Pauli strings

- Circuit synthesis for $\exp(iZ_2Z_1I_0) \cdot \exp(iZ_2Z_1Z_0)$



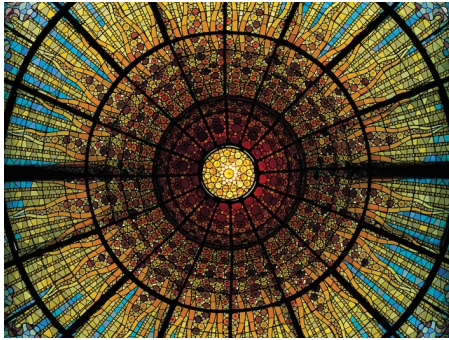
- ❖ Naïve synthesis for each separate kernel
- ❖ No gate cancellation.



- ❖ **Common subtree-centric gate synthesis** for large-scope gate cancellation.
- ❖ CNOTs cancel out with each other.

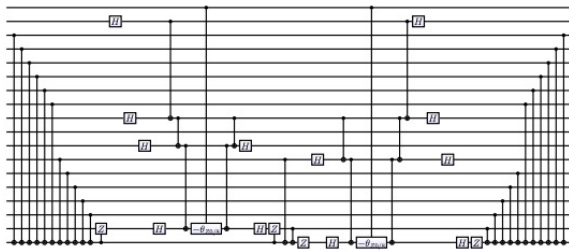
More **active qubits overlapping** between nearby Pauli IR kernels → more gate cancellation.

Moreover



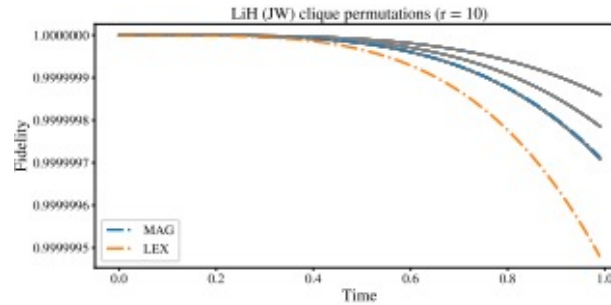
[Livio, 2012]

symmetry preserving



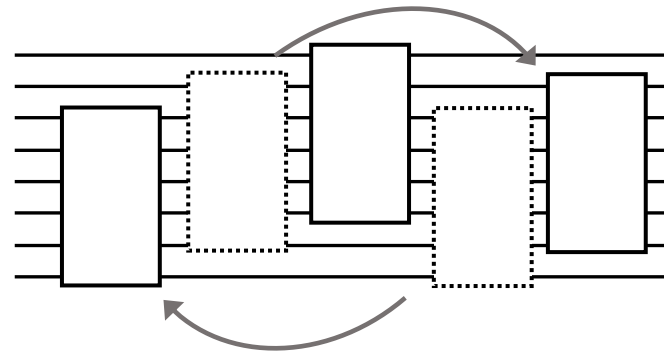
[Hastings et al. 2015]

more gate cancellation



[Gui et al. 2019]

error mitigation

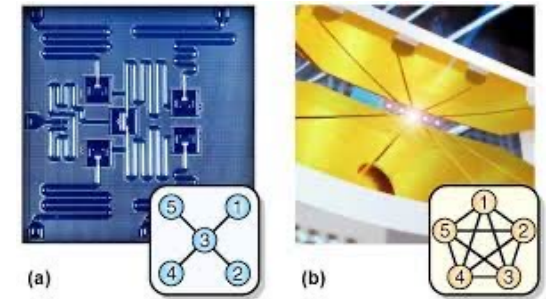


large-scope scheduling

$$\begin{aligned}(a_2^\dagger a_0 - a_0^\dagger a_2) &= \frac{i}{2}(X_2 Z_1 Y_0 - Y_2 Z_1 X_0) \\(a_3^\dagger a_1 - a_1^\dagger a_3) &= \frac{i}{2}(X_3 Z_2 Y_1 - Y_3 Z_2 X_1) \\(a_3^\dagger a_2^\dagger a_1 a_0 - a_0^\dagger a_1^\dagger a_2 a_3) &= \\&= \frac{i}{8}(X_3 Y_2 X_1 X_0 + Y_3 X_2 X_1 X_0 + Y_3 Y_2 Y_1 X_0 + Y_3 Y_2 X_1 Y_0 \\&\quad - X_3 X_2 Y_1 X_0 - X_3 X_2 X_1 Y_0 - Y_3 X_2 Y_1 Y_0 - X_3 Y_2 Y_1 Y_0).\end{aligned}$$

[McArdle et al. 2020]

parameter sharing



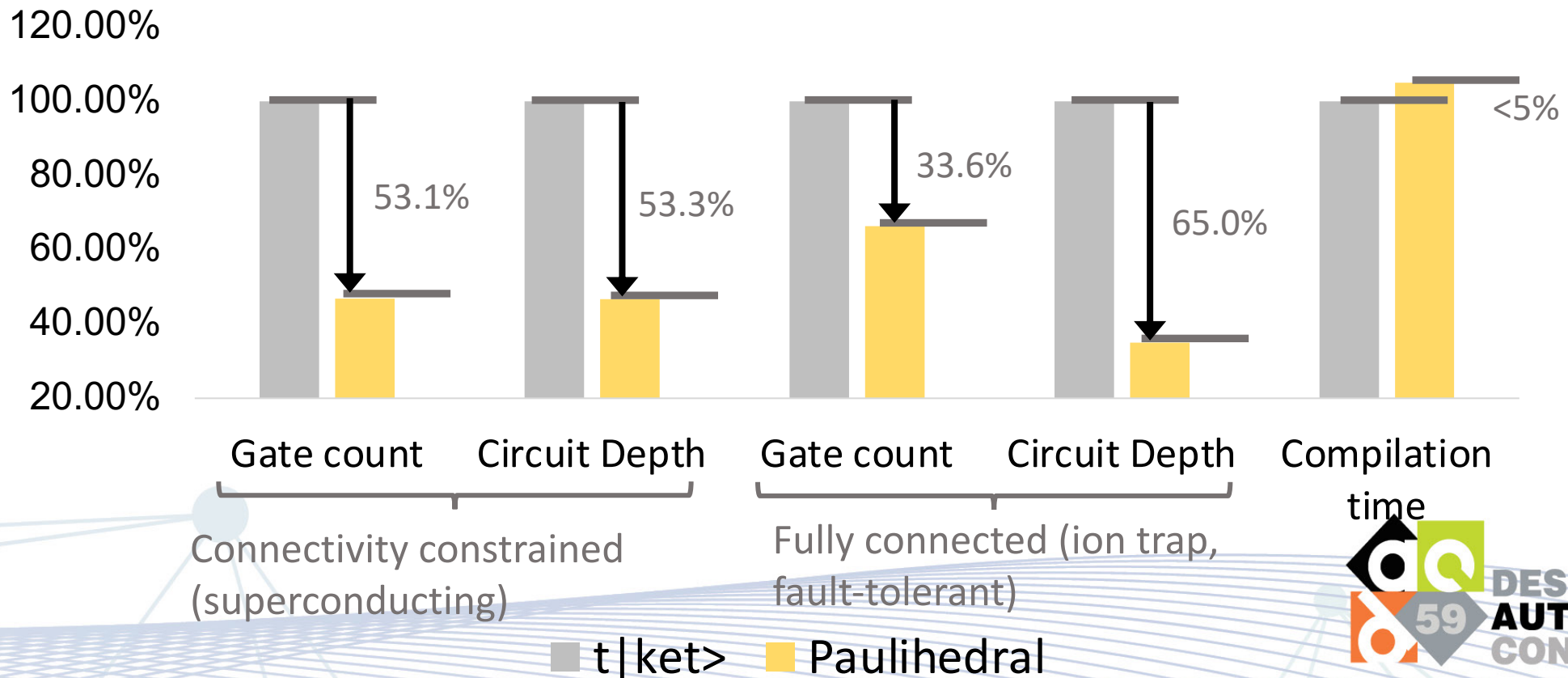
[Linke et al. 2017]

different backends

Please see paper for details

Evaluation

- Benchmarks: molecule/Ising/Heisenberg/random Hamiltonian, UCCSD/QAOA graph ansatz





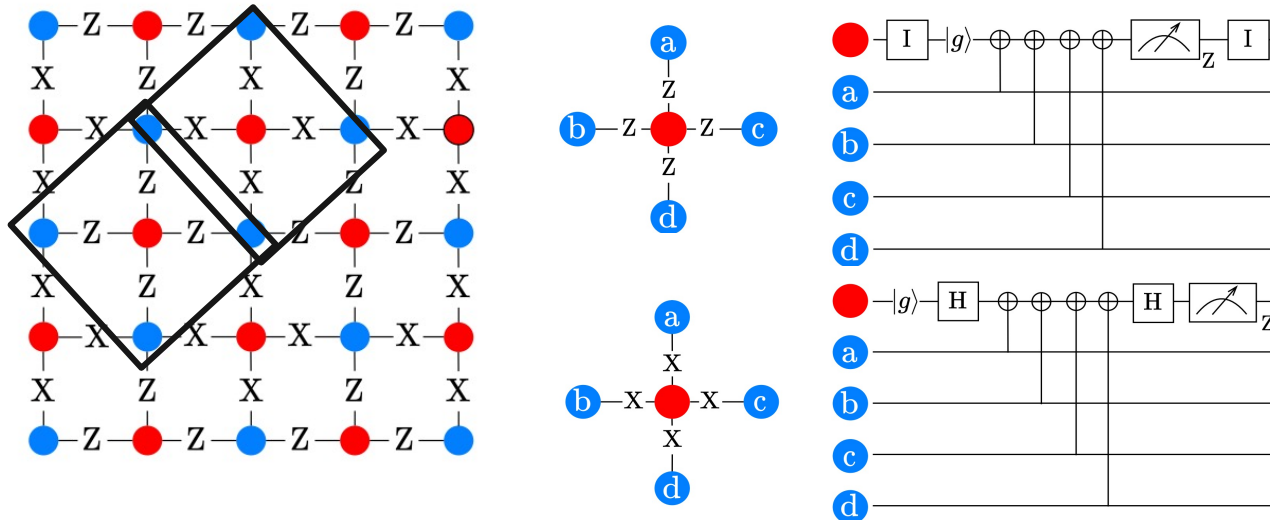
A Synthesis Framework for Stitching Surface Code with Superconducting Quantum Devices

Anbang Wu, Gushu Li, Hezi Zhang, Gian Giacomo Guerreschi,
Yufei Ding, Yuan Xie

ISCA 2022

QEC Program: Surface Code

- Surface code: one of the best QEC in terms of error correction capabilities (up to about 1% error).



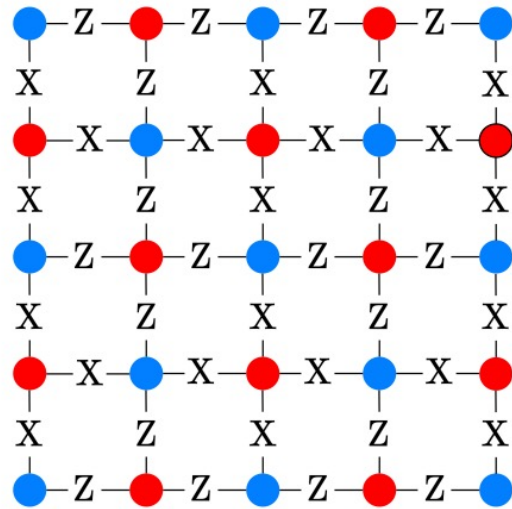
Circuits can be perfectly mapped to the hardware (coupling graph) on the left side.

- 2-D lattice qubit structure: **long-range entanglement** to protect the logic qubit from local noises.

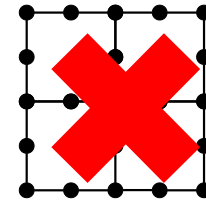
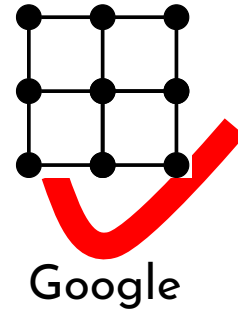
Data qubits (blue): encode the correct subspace for logical operations.

Syndrome qubit (red): ensure data qubits are working collaboratively by checking their X, Z parity.

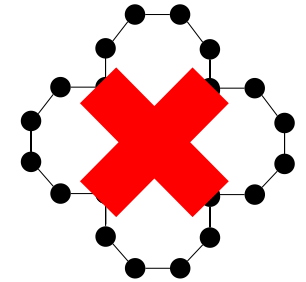
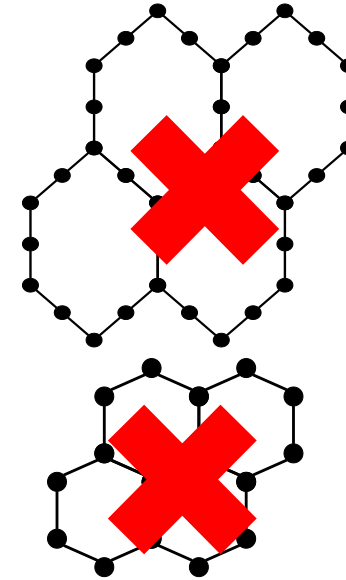
Mismatch between Surface Code and Sparse Architectures



Surface Code



IBM

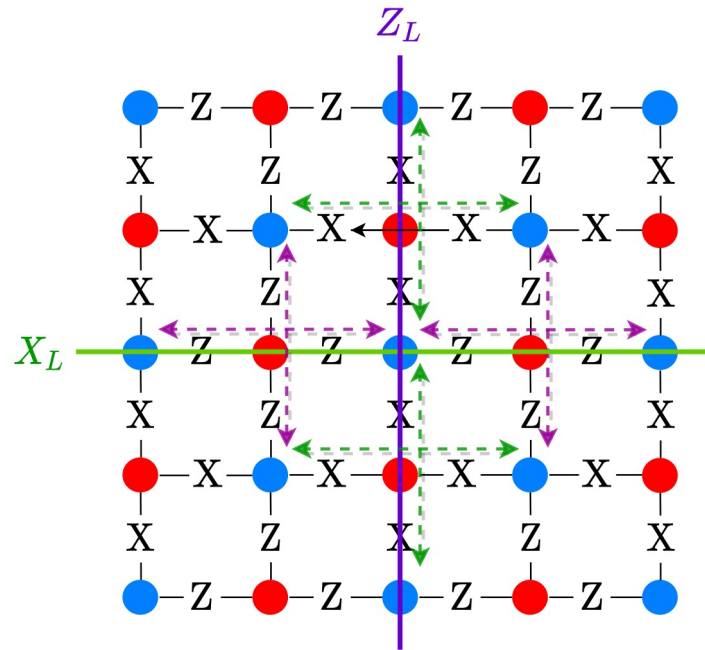
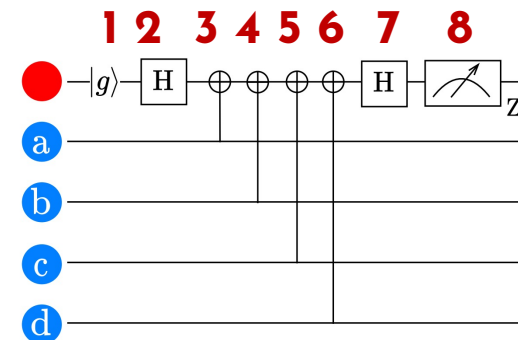
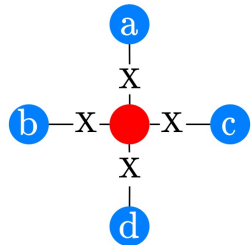
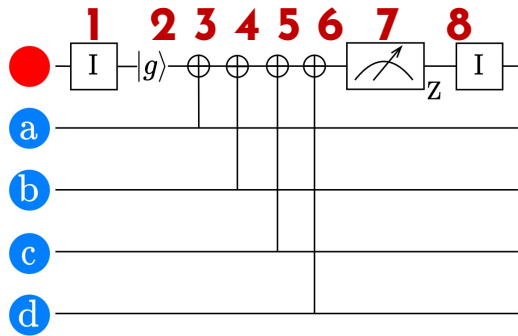
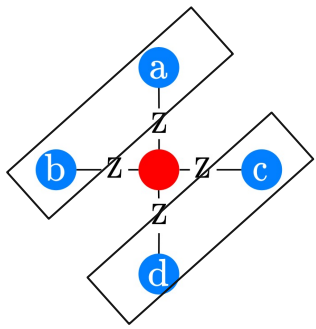


Rigetti

Some recent study designed new QEC codes tailored for these **sparse** architecture.

❖ Can the “mismatch” be mitigated by compiler optimization?

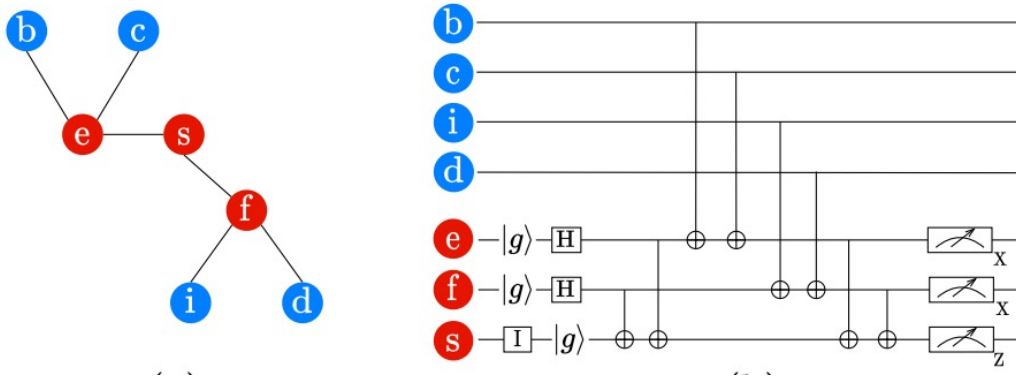
What is Special about QEC program?



- 1) **4-degree qubit**: each syndrome qubit (red) measures the **parity** of 4 data qubits (blue).
- 2) **Fixed data qubit Layout**: moving data qubits would invalidate those high-level logical operations.
- 3) **Stabilizer measurement scheduling**: zigzag (instead of clockwise) gives maximum parallelism.

Our QEC Compiler

- How to resolve the mismatch problem from a compiler's perspective? If so, to what extent?



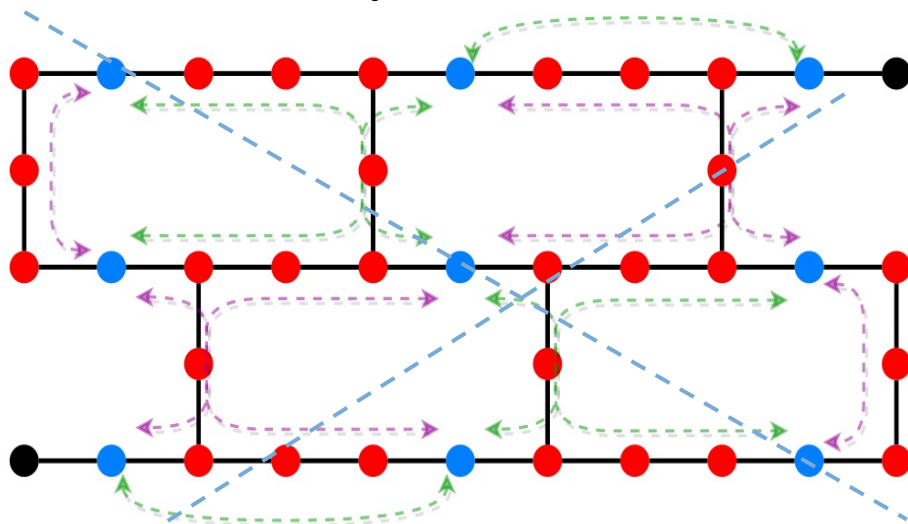
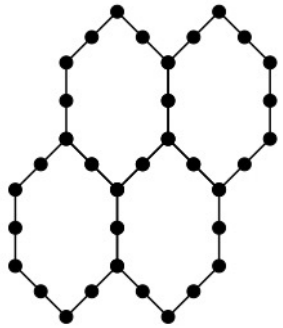
Bridge tree to encode a “**logic**” **syndrome qubit**, and use it to replace a 4-dgree node.
[L. Lao et. al. PRA2020]

- ❖ **Three key submodules** to resolve the surface code mismatch problem:
 1. How are data qubits allocated?
 2. How to find “small and local “ bridge trees?
 3. How to schedule stabilizer measurement circuits?

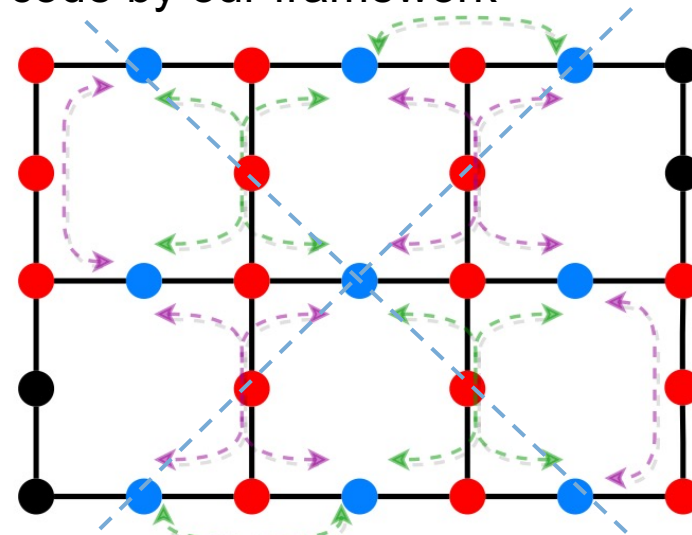
Our QEC Compiler

- We build the **first automated framework** for compiling **surface code** to sparse quantum devices with a **modularized** design.

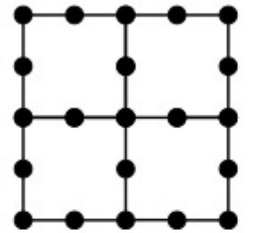
➤ The synthesized distance-3 surface code by our framework



(a) Heavy Hexagon



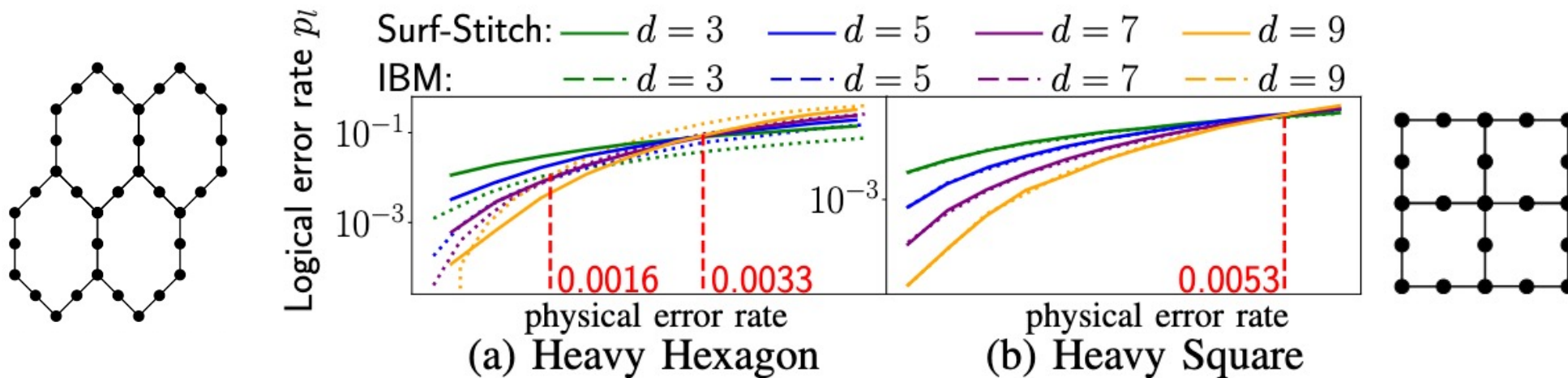
(b) Heavy Square



We could work with different architectures + missing links/qubits.

Performance of Our QEC Compiler

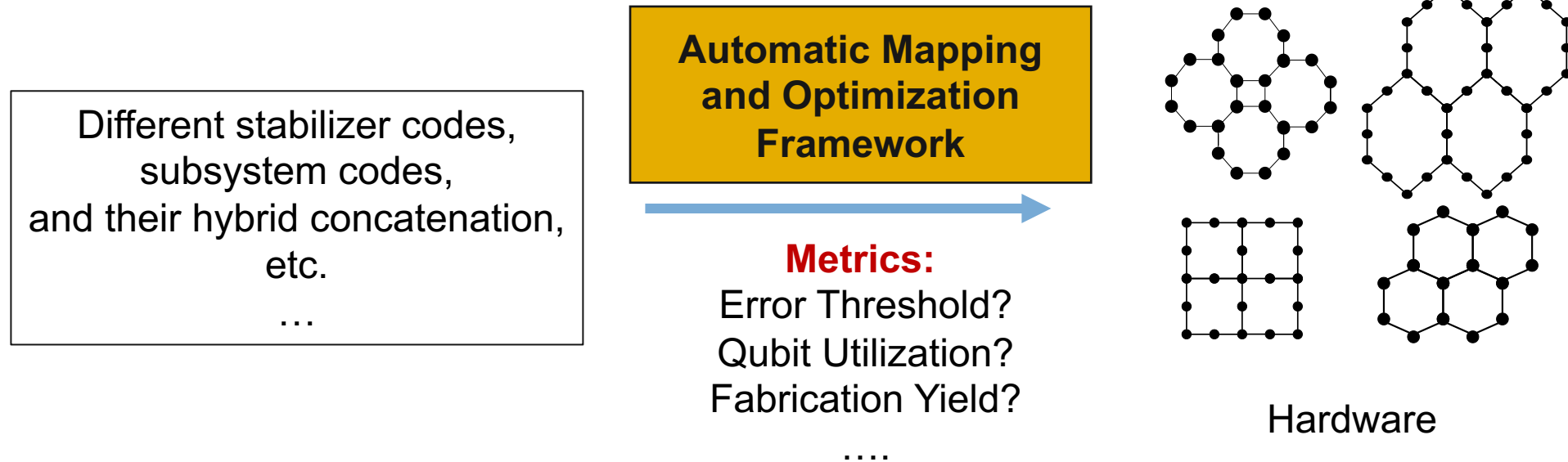
- The *error threshold* of the **compiled surface code** is comparable or even better than IBM's **manually designed** QEC codes tailored for the sparse architectures.



More results in our paper.

Our Vision for Future QEC Development

- General QEC design and mapping could be formulated as a compiler problem.



A compiler framework to automate the designs of **hardware-aware** QEC codes + its associated error decoder!!!

Q & A

- Thank you!